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Use of a failure probability constraint to suggest an initial dose in a phase I cancer clinical trial

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# Original Article

# Use of a failure probability constraint to suggest an initial dose in a phase I cancer clinical trial



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# **ABSTRACT**

The primary objective of a Phase I cancer clinical trial is to determine the maximum tolerated dose of a drug. The "failure probability" was proposed and used as a constraint to help identify a suitable initial dose range. The maximum tolerated dose was then determined based on a  $3 + 3$  cohort-based escalation scheme. Multiple simulations were conducted, and the method was evaluated according to the required sample size and accuracy and precision of maximum tolerated dose estimate. The results indicated that the median of the initial dose range suggested using a failure probability is a suitable initial dose regardless of the dose escalation sequence used for a cancer Phase I study. This initial dose required a smaller sample size and resulted in less bias of the estimated maximum tolerated dose compared with a commonly used initial dose, that is, 10% of the lethal dose. We tested our approach using real dose and toxicity outcome data from two published Phase I studies. These results indicate that adding a failure probability constraint into the calculation of the initial dose range will improve the efficiency of Phase I cancer trials.

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#### 1. Introduction

A Phase I cancer clinical trial is conducted to determine the maximum tolerated dose (MTD) of a drug, which is the highest dose at which only a predefined, acceptable proportion of participants experience dose-limiting toxicity (DLT) [\[1,2\]](#page-7-0).

The MTD is determined using a dose escalation scheme. Two types of escalation schemes are commonly used: cohort-based [\[3,4\]](#page-7-0) and model-based [\[5,6\]](#page-7-0) schemes. The  $3 + 3$  cohort-based scheme (3  $+$  3 design) is widely used owing to its simple method of calculating the numbers of participants who experience DLT. This design starts with a cohort of three participants. If no DLT occurs in this cohort, another three participants are recruited and given the drug at a higher dose. If one DLT occurs, three more participants are recruited at the same dose level. The dose escalation proceeds until at least two DLTs occur at a given dose. In the  $3 + 3$  design, the MTD is the maximum dose at which less than 33% of participants experience DLT [\[7,8\].](#page-7-0)

Common dose escalation sequences are (i) the Fibonacci sequence (FS), in which each dose is the sum of the two previous doses [\[9\];](#page-7-0) (ii) the smoothed modified Fibonacci sequence (SMFS), which is similar to the FS but with a modification, relative increments are 100%, 67%, 50%, 40%, and 33% thereafter, to avoid DLT with subsequent higher doses [\[10,11\];](#page-7-0) (iii) the golden ratio increment sequence (GRIS), which is a 61.8% increment in each dose, the percentage obtained from the convergence of the FS [\[12\]](#page-7-0); and (iv) the multiple constant dose increment sequence (MCDIS), in which the dose escalates by a constant amount, usually a multiple of the initial dose  $[12-15]$  $[12-15]$ .

The initial dose in a Phase I trial is usually determined from preclinical animal studies and is calculated based on 10% of lethal dose  $(LD_{10})$  in rodents, one-sixth of the highest nonseverely toxic dose in non-rodents, or no observed adverse effect levels in tested animals and body surface area  $[16-18]$  $[16-18]$ . Too low an initial dose is unsatisfactory because it may yield a low number of DLTs and require a large number of participants to determine the MTD. Too high an initial dose is also unsatisfactory because it may yield too many DLTs and fail to find the MTD. Thus, choosing the correct initial dose is of the utmost importance in a Phase I clinical trial.

The use of probability functions to calculate the likelihood of DLT as a function of dose has been proposed in a modelbased approach [\[5\]](#page-7-0). Even if the unknown toxicity function can be arbitrarily assigned, the appropriate parameters in the function can only be solved with additional information; once the parameters have been estimated, however, MTD can be estimated. Theoretically, if a  $3 + 3$  design is used, the MTD is the dose at which the probability of DLT is less than but close to 0.33. However, a review of published Phase I trials with a  $3 + 3$  design reported that the probability of DLT at MTD was between 0.17 and 0.26  $[19]$ . The aim of this study was that an initial dose should be suggested to correspond to a more accurate DLT function and its dose escalation sequence.

The initial dose should be selected with caution and with particular consideration given to obtaining the appropriate MTD. Here we propose an approach that uses failure probability (FP) as a constraint to help choose the initial dose. We hypothesize that use of FP to suggest initial dose would reduce the bias associated with the MTD and reduce the required sample size to determine MTD.

## 2. Methods

#### 2.1. Dose-limiting toxicity probability function

Non-decreasing functions such as hyperbolic tangent functions, probit functions, and logit functions have been used to represent the relation between dose and toxicity [\[5,6,20\].](#page-7-0) Among them, the logit function is most common owing to its flexibility. The logit function is presented in Equation (1):

$$
P(DLT|Dose = d_j) = p_j = \frac{e^{\alpha + \beta d_j}}{1 + e^{\alpha + \beta d_j}}, \infty > \alpha > -\infty, \beta > 0,
$$
 (1)

where  $d_j$  denotes the  $j^{\text{th}}$  dose corresponding to the specific initial dose and  $j = 1, 2, ..., J$ , and  $\alpha$  and  $\beta$  are unknowns that can be estimated. We constrained parameter  $\alpha$  in the logit function to be greater than a constant in order to ensure a positive DLT probability when the dose is zero. We then estimated  $\beta$  with  $d_1$ , where  $d_1$  is obtained based on LD<sub>10</sub>. DLT probability at  $d_1$  is 0.01. If DLT probability is overestimated, then the MTD estimate will be conservative. Thus, values of  $\beta$ are critical to the outcome of the logit function.

#### 2.2. Failure probability

FP can be regarded as the expected probability of a particular dose being the MTD if the initial dose was selected appropriately. It is defined as the probability that MTD fails to be determined given J dose levels with a particular initial dose,  $d_1$ , as shown in Equation (2):

$$
FP = P(MTD < d_1) + P(MTD \ge d_j) = T^{(1)} + \prod_{j=1}^{J} (1 - T^{(j)}),
$$
 (2)

where  $T^{(j)}$  is the probability of stopping the escalation at  $d_j$ . Lin and Shih [\[4\]](#page-7-0) calculated T<sup>(j)</sup> from Bin(3,  $p_i$ ) in a 3 + 3 design, which is simply a cumulative probability from the binomial distribution.

We defined P(MTD =  $d_i$ ) as the conditional probability that  $d_i$ is the MTD, as presented in Equation (3):

 $P(MTD = d_j)$  $= P\frac{\text{(exrelation at dose level} \le d_j; \text{stop exrelation at dose level } d_{j+1})}{P(MTD \text{ is determined)}}$  $P(MTD)$  is determined)  $\equiv$  $T^{(j+1)}$   $\prod^j$  $t=1$  $\left( 1-T^{(t)}\right)$  $\frac{\frac{1}{\mathsf{t} - 1}}{1 - \left(\mathsf{T}^{(1)} + \prod\limits_j^J (1 - \mathsf{T}^{(\mathsf{t})})\right)}, j = 1,...,J-1.$ 

 $t=1$ 

<span id="page-3-0"></span>

Fig.  $1$  – Failure probability (FP). (A) FP versus dose for each of the four dose escalation sequences calculated using a logit DLT function with  $\alpha = -5.3$  and  $\beta = 0.695$ . The horizontal line represents 20% FP. The range indicated by the two vertical dashed lines represents the suggested initial dose range for SMFS. (B) FP versus dose calculated using a logit DLT function with  $\alpha = -5.3$  and various values of  $\beta$ . Horizontal line represents 20% FP. DLT = dose-limiting toxicity; SMFS = smoothed modified Fibonacci sequence.

Consideration of FP increasing the confidence in MTD is successfully determined before the start of the trial. A range of suitable initial doses can be determined by solving the inequality equation that FP is less than a certain threshold.

#### 2.3. Sample size

The expected sample size required at each dose level was derived by Lin and Shih  $[4]$ , and we extended this calculation to determine the expected sample size required for the whole trial (N) as shown in Equation  $(4)$ :

range and select the initial dose for use in simulations. DLT probability for each dose escalation sequence (FS, SMFS, GRIS, or MCDIS) was generated from the assumed true probability using the logit function with random deviation  $\varepsilon$ <sub>j</sub>. DLT probability was represented as shown in Equation (5):

$$
P(DLT|Dose = d_j) = \frac{e^{\alpha + \beta d_j + \epsilon_j}}{1 + e^{\alpha + \beta d_j + \epsilon_j}},
$$
\n(5)

where  $\varepsilon_j^{\text{iid}} \sim N(0, \sigma^2)$  and  $\sigma^2$  represents the variability in reception to the toxic response of the drug for an individual at  $d_i$ .

$$
E(N) = \sum_{j=1}^{J-1} \left[ E(n_j | MTD = d_j) P(MTD = d_j) \right]
$$
\n
$$
= \sum_{j=1}^{J-1} \left\{ \left[ 3(j+1)3 \sum_{k=1}^{j} \left( \frac{U^{(k)} - T^{(k)}}{1 - T^{(k)}} \right) + 3 \frac{U^{(j+1)}}{T^{(j+1)}} \frac{U^{(j+1)} - T^{(j+1)}}{1 - U^{(j+1)}} \right] \frac{T^{(j+1)}}{1 - T^{(1)} - \prod_{j=1}^{J} (1 - T^{(j)})} \right\},
$$
\n(4)

where  $E(n_j | MTD = d_j)$  is the expected sample size with  $d_j$  is the MTD, and  $U^{(j)} = 1 - \begin{pmatrix} 3 \\ 0 \end{pmatrix}$ 0  $(p_j^0(1-p_j)^3$  is the probability that at least one DLT occurred at  $d_j$  ( $j = 1, 2, ..., J - 1$ ).

# 2.4. Simulation studies

Simulations were carried out using R version 2.15.1 (The R Foundation for Statistical Computing, Vienna, Austria). We used 20% as the FP constraint to determine the initial dose

Parameters  $\alpha = -5.3$  and  $\beta = 1.927, 1.211, 0.883, 0.816,$  and 0.695 were used to ensure low DLT probability at dose zero and a smooth, increasing trend of the logit function. Simulations were performed with  $\sigma^2$  ranging from 0.2 to 2.0 in increments of 0.2.

The probability of DLT occurrence was generated from Uniform(0, 1). A DLT was regarded to have occurred if the generated probability was smaller than the true DLT probability, which was generated from Equation  $(5)$ . The 3 + 3 design was followed to determine whether the dose should be raised <span id="page-4-0"></span>to a higher level. Simulations were iterated until MTD had been successfully estimated 1000 times for each initial dose. Simulated expected overall sample size, average number of DLTs, average MTD estimate, and accuracy of MTD estimate (i.e., percentage bias) were obtained. Percentage bias is a common metric in evaluating the simulation [\[21\]](#page-7-0) and was defined as  $\left(d_{\text{MTD}}-d_{\text{MTD}}\right)/d_{\text{MTD}}\times 100\%$ , where  $d_{\text{MTD}}$  is the estimate of MTD,  $\overline{d}_{\rm MTD} = 1/_{1000} \sum_{i=1}^N$  $i=1$  $\sum\limits_{i=1}^{1000} \,\widehat{d}_{\mathrm{MTD},i}$ , and  $d_{\mathrm{MTD}}$  is the true MTD. Theoretically,  $d_{\text{MTD}}$  can be solved in the DLT functions and used as a reference value for simulation.

Data from two published studies were used to compare the proposed method to real data.

# 3. Results

#### 3.1. Simulation studies

The initial dose ranges obtained for each dose escalation sequence are displayed in [Fig. 1A](#page-3-0). The initial dose range was



Fig.  $2$  – True percentage bias with different initial dose ranges. The percentage bias calculated from the true DLT function with  $\alpha = -5.3$  and  $\beta = 0.883$ . The x axis is the percentile of the derived initial dose range that was used as the initial dose. The blue bar represents the initial dose suggested by the true DLT function. The percentage bias was similar between the 10th and 50th percentiles of the derived initial dose range. If the wrong DLT function (e.g., the same  $\alpha$  value and  $\beta = 0.695, 0.816, 1.211, 1.927$ ) was used to estimate initial dose, the suggested initial dose range would be represented by the red bar that overlaps the true initial dose range. The suggested initial dose was appropriate even if the estimate of  $\beta$  deviated from the true value of  $\beta$  because the difference in percentage bias between the 10th and 50th percentiles of the derived initial dose range was small and the suggested initial dose range overlapped the initial dose range that suggested from the true DLT function.  $DLT =$  dose-limiting toxicity.

obtained by drawing a horizontal line at 20% of FP. The FP values calculated for the SMFS dose escalation sequence with different initial doses using different scale parameters in the logit DLT function are displayed in [Fig. 1B](#page-3-0). The initial dose range became smaller as  $\beta$  increased for the same dose escalation sequence. The initial dose range is shown in Fig. 2.

The sample size, number of DLTs, percentage bias, and precision for each dose escalation sequence are displayed in figures for every 10th percentile increment of the initial dose range. Variables were calculated in this way because the absolute values of the initial dose ranges were not the same across the four dose escalation sequences and across different  $\beta$  values. Only the results obtained with  $\alpha = -5.3$ ,  $\beta = 0.695$ , and  $\sigma = 1.2$  are presented because other results were similar.

[Fig. 3A](#page-5-0) shows the total sample size and number of DLTs in the simulated Phase I trial. These results indicated that 9.5 participants would be needed and DLT would be expected in 2.8 participants if SMFS was used and the 50th percentile (median) of the derived initial dose range was used as the initial dose. The required sample size decreased when the initial dose increased within the derived initial dose range. The results indicated that smaller sample sizes were needed when SMFS or MCDIS was used as the dose escalation sequence than when FS or GRIS was used as the dose escalation sequence. The average number of participants with DLT was approximately three in each simulation for all doses, as expected for a  $3 + 3$  design.

The percentage bias of MTD was always negative because estimates of MTD were always lower than the true MTD. For simplicity, the percentage bias was expressed with positive values in the simulation results. The percentage bias for all derived initial doses was between 15% and 40% for all dose escalation sequences [\(Fig. 3B](#page-5-0)). If the initial dose was between the 10th and 60th percentile of the derived initial dose range then the percentage bias was similar for all dose escalation sequences [\(Fig. 3](#page-5-0)B). If the initial dose was below the 10th percentile of the derived initial dose range, the percentage bias was greater [\(Fig. 3](#page-5-0)B). GRIS yielded a smaller percentage bias when the initial dose was above the median of the derived initial dose range. In all four dose escalation sequences, the smallest percentage bias occurred when the initial dose was above the 90th percentile of the derived initial dose range.

Precision was defined as the number of successful simulations (i.e., simulations that achieved the goal of establishing an MTD) divided by the total number of runs in the simulation. Higher precision represents a higher probability that the initial dose chosen in that particular sequence would eventually establish an MTD. Precision was greater than 95% if the initial dose was between the 10th and 50th percentile of the derived initial dose range [\(Fig. 3](#page-5-0)C).

When taking all four metrics into considerations, results of simulation with an FP constraint suggested that the initial dose should be between the 10th and 50th percentile of the derived initial dose range for all four dose escalation sequences.

We performed simulations in which we considered various values of  $\beta$  in the logit function and showed that the calculated initial dose range changed smoothly with  $\beta$ . The suggested initial doses (10th to 50th percentile of the derived

<span id="page-5-0"></span>

Fig. 3 - Sample size, number of DLTs, and bias and precision of MTD estimate versus percentile of the initial dose range. (A) Sample size and number of DLTs, (B) percentage bias, and (C) precision of the MTD estimate calculated using a logit DLT function with  $\alpha = -5.3$  and  $\beta = 0.695$  for each for the four dose escalation sequences. The individual deviation of DLT probability was distributed as N(0, 1.44). The x axis is the percentile of the derived initial dose range that was used as the initial dose. The left y axis in (A) represents the sample size used in the escalation process, and the right y axis in (A) represents the number of DLTs that occurred in the escalation process.  $DLT =$  dose-limiting toxicity; MTD  $=$  maximum tolerated dose.

initial dose range) were greatly overlapped when the range was calculated with different values of  $\beta$ . Most importantly, the simulation demonstrated that the total sample size, number of DLTs, and percentage bias were similar across different values of  $\beta$  when the median of the initial dose range was selected as the initial dose. The metrics derived from the simulation provide strong evidence for this (Fig. 4).

[Fig. 5](#page-6-0) demonstrates that the relation among variability  $(\sigma)$ and sample size, number of DLTs, and percentage bias was similar for all four dose escalation sequences. The required sample sizes were similar for all assumed values of  $\sigma$ . However, the percentage bias of the estimated MTD increased with variability. These findings were the same for all four dose escalation sequences.

#### 3.2. Comparison with published data

The sample size and number of DLTs obtained with the proposed simulation method were compared with two published Phase I cancer trials: the use of holmium-166 radioembolization  $(166Ho-radioembolization)$  for patients with unresectable, chemorefractory liver metastases [\[14\]](#page-7-0) and the use of vandetanib for patients with recurrent malignant gli-omas [\[15\]](#page-7-0). Both studies had a  $3 + 3$  design with an MCDIS dose escalation sequence.

The  $^{166}$ Ho-radioembolization study used 20 Gy as the initial dose and found 60 Gy to be the MTD. The total sample size was 15, and there were three DLTs [\[14\].](#page-7-0) Using the proposed approach with FP = 20% and MCDIS, the derived values of  $\alpha$ 



Fig. 4 – Sample size, number of DLTs, and accuracy of  $\widehat d_{\rm MTD}$  with different  $\beta$  values. A logit DLT function with  $\alpha=-$  5.3 and different  $\beta$  values was used for all dose escalation sequences. The median of the derived initial dose range was used as the initial dose, and the individual deviation of the DLT probability was distributed as N(0, 1.44). The left y axis in (A) represents the sample size used in the escalation process, and the right y axis in (A) represents the number of DLTs that occurred in the escalation process.  $DLT =$  dose-limiting toxicity.

<span id="page-6-0"></span>

Fig. 5 – Sample size, number of DLTs, and accuracy of  $\widehat d_{\rm MTD}$  with different  $\sigma$  values. A logit DLT function with  $\alpha=-$  5.3 and  $\beta = 0.695$  and different individual  $\sigma$  values was used for all dose escalation sequences. The median of the derived initial dose range was used as the initial dose. The left y axis in (A) represents the sample size used in the escalation process, and the right y axis in (A) represents the number of DLTs that occurred in the escalation process. DLT  $=$  dose-limiting toxicity.

and  $\beta$  were  $-5.29$  and 0.07, and the initial dose range was 11.43 $-51.53$  Gy. If the median of this range (30 Gy) was used as the initial dose, our method predicted an MTD of 60 Gy with a required sample size of 9.7 and 2.8 DLTs.

The vandetanib study used 100 mg as the initial dose and found 100 mg to be the MTD. The total sample size was 10, and there were three DLTs [\[15\]](#page-7-0). Using the proposed approach with FP  $=$  20% and MCDIS, the derived values of  $\alpha$  and  $\beta$  were  $-5.29$ and 0.024, and the initial dose range was 33.33-150.32 mg. If the median of this range (90 mg) was used as the initial dose, our method predicted an MTD of 180 mg with a required sample size of 9.3 and 2.7 DLTs. Some other studies confirmed that the dose can be tolerated as high as 300 mg [\[22,23\].](#page-7-0)

#### 4. Discussion

This study proposed and used an FP constraint and performed several simulations to determine MTD using four different dose escalation sequences. The results suggested that the proposed method could be helpful for determining MTD with a smaller sample size and less bias.

This study used a logit function to model the relation between dose and toxicity. The scale parameter  $\beta$  in the logit function was estimated using a dose derived from animal studies. The value of  $\beta$  is critical to the study because it greatly affects the shape of the logit function and thus affects DLT probability at each dose level.  $\beta$  represents the degree of instantaneous increment in DLT probability. Mathematically, it is inversely related to the size of the initial dose range. The dose ranges calculated with different values of  $\beta$  overlapped [\(Fig. 2](#page-4-0)), and the dose range from one particular  $\beta$  estimate was largely covered by other  $\beta$  estimates with the same dose escalation sequence, suggesting that the initial dose estimate

may be appropriate even when the estimate of  $\beta$  deviates from its true value.

Notably, with FS, SMFS, and MCDIS, the bias decreased to 20% when the initial dose was between the 70th and 100th percentile of the initial dose range [\(Fig. 3](#page-5-0)B). With each dose escalation, the second dose is twice as large as the initial dose. Each initial dose is MTD if the DLT probability of the initial dose is lower than the target DLT probability and the DLT probability of the second dose is higher than the target DLT probability. In this situation, the bias decreases as initial dose increases. Although the MTD will have smaller bias and require a smaller sample size, the precision of the simulation with such initial doses will become much lower, reducing the chances of successfully determining MTD.

In our method, the dose increment in MCDIS was dependent on the initial dose. Some studies have used a constant dose increment but different magnitude of initial dose [\[24,25\],](#page-7-0) and other studies have increased the dose with irregular increments [\[26,27\]](#page-7-0). In practice, the dose increments should be determined according to the pharmacological characteristics of the drug. However, the relative increase of subsequent dose increments will not change or will decrease for all four dose escalation sequences.

There are a few limitations to this study. First, the proposed method heavily relies on toxicity information from animal studies, that is,  $LD_{10}$ . Toxicity information from animal studies is limited and can sometimes be confidential as it is acquired in the early stages of drug development. Thus, one should be cautious when estimating  $\alpha$  and  $\beta$  in the logit function. Second, we only considered a logit DLT function. Although this is the most widely used function, other functions can be used such as a hyperbolic tangent function. Third, all MTD estimates heavily depend on the escalation scheme. The  $3 + 3$  design is one of the most common schemes in use and is a special case of the  $A + B$  design [\[4\],](#page-7-0) but our proposed

<span id="page-7-0"></span>method can also be extended to other, more complicated schemes.

Our proposal of adding an FP constraint into the suggestion of the initial dose will help the design of Phase I cancer trials, making them more efficient and more economical. In general, our study suggests that the median of the derived initial dose range should be chosen as the initial dose of a Phase I study regardless of the dose escalation sequence used.

# Conflicts of interest

All contributing authors declare no conflicts of interest.

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#### references

- [1] [Modi M. Dose-finding studies in phase I and estimation of](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref1) [maximally tolerated dose. In: Ting N, editor. Dose finding in](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref1) [drug development. New York: Springer; 2006. pp. 30](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref1)-[48](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref1).
- [2] [Ivanova A. Dose-finding in oncology](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref2)  $-$  [nonparametric](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref2) [methods. In: Ting N, editor. Dose finding in drug](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref2) [development. New York: Springer; 2006. pp. 49](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref2)-[58.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref2)
- [3] [Storer BE. Design and analysis of phase 1 clinical trials.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref3) [Biometrics 1989;45:925](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref3)-[37.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref3)
- [4] [Lin Y, Shih WJ. Statistical properties of the traditional](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref4) [algorithm-based designs for phase 1 clinical trials.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref4) [Biostatistics 2001;2:203](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref4)-[15.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref4)
- [5] [O'Quigley J, Pepe M, Fisher L. Continual reassessment](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref5) [method: a practical design for phase 1 clinical trials in](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref5) [cancer. Biometrics 1990;46:33](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref5)-[48.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref5)
- [6] [Babb J, Rogatko A, Zacks S. Cancer phase I clinical trials:](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref6) [efficient dose escalation with overdose control. Stat Med](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref6) [1998;17:1103](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref6)-[20](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref6).
- [7] [Carter SK. Study design principles for the clinical evaluation](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref7) [of new drugs as developed by the chemotherapy programme](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref7) [of the National Cancer Institute. In: Staquet M, editor. The](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref7) [design of clinical trials in cancer therapy. Brussels: Editions](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref7) [Scientifique Europeennes; 1973. pp. 242](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref7)-[89](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref7).
- [8] [Von Hoff DD, Kuhn J, Clark GM. Design and conduct of phase](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref8) [1 trials. In: Buyse ME, editor. Cancer clinical trials: methods](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref8) [and practice. Oxford: Oxford University Press; 1984.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref8) [pp. 210](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref8)-[20](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref8).
- [9] [Bellman RE. Topics in pharmacokinetics, III: repeated dosage](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref9) [and impulse control. Math Biosci 1971;12:1](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref9)-[5.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref9)
- [10] [Goldsmith MA, Slavik M, Carter SK. Quantitative prediction](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref10) [of drug toxicity in humans from toxicology in small and large](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref10) [animals. Cancer Res 1975;35:1354](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref10)-[64.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref10)
- [11] [Lutz E. Overview of phase I trials. In: Crowley J, editor.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref11) [Handbook of statistics in clinical oncology. 2nd ed. New](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref11) [York: Marcel Dekker; 2005. pp. 1](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref11)-[34](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref11).
- [12] [Spilker B. Guide to clinical trials. New York: Raven Press;](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref12) [1991.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref12)
- [13] [Curry III EA, Murry DJ, Yoder C, et al. Phase I dose](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref13) [escalation trial of feverfew with standardized doses of](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref13) [parthenolide in patients with cancer. Invest New Drugs](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref13) [2004;22:299](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref13)-[305.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref13)
- [14] [Smits MLJ, Nijsen JFW, van den Bosch MAAJ, et al.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref14) [Holmium-166 radioembolisation in patients with](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref14) [unresectable, chemorefractory liver metastases \(HEPAR](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref14) [trial\): a phase 1, dose-escalation study. Lancet Oncol](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref14) [2012;13:1025](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref14)-[34.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref14)
- [15] [Fields EC, Dame D, Gaspar LE, et al. Phase I dose escalation](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref15) [trial of vandetanib with fractionated radiosurgery in patients](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref15) [with recurrent malignant gliomas. Int J Radiat Oncol Biol](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref15) [Phys 2012;82:51](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref15)-[7.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref15)
- [16] Food [and Drug Administration. Guidance for industry:](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref16) [estimating the maximum safe starting dose in initial clinical](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref16) [trials for therapeutics in initial adult healthy volunteers.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref16) [Rockville, MD, U.S.A.: Food and Drug Administration; 2005.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref16)
- [17] [International Conference on Harmonisation \(ICH\). S9:](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref17) [nonclinical evaluation for anticancer pharmaceuticals.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref17) [Rockville, MD, U.S.A.: Food and Drug Administration; 2010.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref17)
- [18] [Wang YF, Huang HY, Chiu YW, et al. Evaluation of](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref18) [multi-strain lactobacillus capsule on gastric emptying](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref18) [function by Tc-99m scintigraphy in a crossover](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref18) [placebo-controlled clinical trial. J Food Drug Anal](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref18) [2012;20:653](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref18)-[60](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref18).
- [19] Ivanova A. Escalation, up-and-down and  $A + B$  designs for dose finding trials. Stat Med  $2006;25:3668-78$ .
- [20] [Faries D. Practical modifications of the continual](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref20) [reassessment method for phase 1 clinical trials. J Biopharm](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref20) [Stat 1994;4:147](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref20)-[64](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref20).
- [21] [Burton A, Altman DG, Royston P, et al. The design of](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref21) [simulation studies in medical statistics. Stat Med](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref21) [2006;25:4279](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref21)-[92.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref21)
- [22] [Heymach JV, Paz-Ares L, De Braud F, et al. Randomized phase](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref22) [II study of vandetanib alone or with paclitaxel and](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref22) [carboplatin as first-line treatment for advanced non-small](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref22)[cell lung cancer. J Clin Oncol 2008;26:5407](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref22)-[15](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref22).
- [23] [Holden SN, Eckhardt SG, Basser R, et al. Clinical evaluation of](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref23) [ZD6474, an orally active inhibitor of VEGF and EGF receptor](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref23) [signaling, in patients with solid, malignant tumors. Ann](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref23) [Oncol 2005;16:1391](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref23)-[7](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref23).
- [24] [Beldner MA, Sherman CA, Green MR, et al. Phase I dose](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref24) [escalation study of vinorelbine and topotecan combination](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref24) [chemotherapy in patients with recurrent lung cancer. BMC](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref24) [Cancer 2007;7:231.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref24)
- [25] [Storniolo AM, Pegram MD, Overmoyer B, et al. Phase I dose](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref25) [escalation and pharmacokinetic study of lapatinib in](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref25) [combination with trastuzumab in patients with advanced](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref25) [ErbB2-positive breast cancer. J Clin Oncol 2008;26:3317](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref25)-[23.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref25)
- [26] [Yamada K, Yamamoto N, Yamada Y, et al. Phase I dose](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref26)[escalation study and biomarker analysis of E7080 in patients](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref26) [with advanced solid tumors. Clin Cancer Res](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref26) [2011;17:2528](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref26)-[37.](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref26)
- [27] [Deeken JF, Slack R, Weiss GJ, et al. A phase I study of](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref27) [liposomal-encapsulated docetaxel \(LE-DT\) in patients with](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref27) [advanced solid tumor malignancies. Cancer Chemother](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref27) [Pharmacol 2013;71:627](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref27)-[33](http://refhub.elsevier.com/S1021-9498(14)00029-5/sref27).